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# Modelling and Simulation of Pitting Corrosion

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## ABSTRACT

Pitting corrosion is one of the most dangerous corrosion types that cause accelerated metal dissolution due to a breakdown of passive protective film on the metal surface. A mathematical simulation of pitting carbon steel corrosion in 1M sodium chloride solution was studied in this work. The commercial software (COMSOL Multiphysics 3.5a) was used to solve the equations that govern this problem. A two-dimensional model that allows the prediction of pit growth of the propagation stage was developed. The simulation model's extracted results show how different parameters such as initial concentration of species, initial pH, different chemical and electrochemical reactions, and range of potential affect the current density and compare the result with the Pourbaix diagram of iron.

## KEYWORDS

COMSOL, pitting corrosion, Mathematical model

## INTRODUCTION

Pitting corrosion is a form of localized corrosion, where the rate of corrosion in certain areas is higher than in others [1-8]. Pitting corrosion can be seen in certain alloys with a passive film on their surface that protects them from general corrosion. Pitting degradation occurs in some of the most widely used alloys, such as stainless steel and aluminium alloys. Corrosion pits of various shapes and sizes, some of which are "hidden" by a perforated cover, may grow wide and cause catastrophic failure in infrastructure systems subjected to mechanical loadings, such as turbine blades bridges, pipelines, and nuclear power plants [9-11]. Corrosion pits regulated by chemical reactions and determined by environmental and mechanical loading conditions across length scales may result in embrittlement (loss of ductility) and major strength decreases [12]. Computational simulations can now implement mathematical models to replicate complicated multi-physics processes with high resolution, thanks to technological advancements in recent decades and a significant rise in computing capacity. Once optimized and accepted against carefully performed studies, computer models will broaden the scope of laboratory investigations to more practical settings and duration and time scales that would be impossible to examine otherwise. These models are mathematical, and they can predict pit depth over time based on those input parameters [13]. Knowing that defeat does not often start from the pitting bottom, more thorough experiments are warranted for learning the capacity to predict failures and then design against them [14]. Models use various computational approaches to solve the pitting mechanism's advancement in more detail: the development of pits' form and composition, the amount of various chemical species within and outside of the trap, the distribution of electrical potential across the domain of interest, etc. Reactions kinetics at the degradation front and the pits' chemical species' transportation kinetics are generally taken as the basis for these models.

## COVERING EQUATION

The Nernst-Planck Equation(N-P), as defined in eq (1), is often utilized to explain ion transfer since convection, migration, and diffusion in the ion transport phase. Each ion's movement because of the device's potential electric fields is believed to be independent of the diffusion term [15].

$$\frac{\partial [i]}{\partial t} = D_i \nabla^2 [i] + Z_i U_i F \nabla ([i] \nabla \Phi) + R_i \quad (1)$$

Where  $[i]$  is the concentration of species  $i$ ,  $D$  is the effective diffusion coefficient,  $Z$  is the charge number,  $U_i$  is the mobility (given that  $U_i = \frac{D_i}{RT}$ ),  $R$  is the production rate/depletion of  $i$ , and  $\nabla\Phi$  is the potential gradient. The Butler–Volmer formula, which gives an average free-energy implementation of charge transfer, but does not analyze the particular processes involved in the transfer, is included in most electrical and chemical kinetic models. The Butler-Volmer equation, which represents the current density at an electrode in terms of the overpotential, describes an electrochemical reaction rate [16]. The form of Butler–Volmer formula as specified in eq (2) below:

$$i = i_0 \left( \exp \left[ a_1 F \frac{(V_m - \Phi)}{RT} \right] \exp \left[ -a_2 F \frac{(V_m - \Phi)}{RT} \right] \right) \quad (2)$$

Where:  $i$  denote electrode current density ( $A/m^2$ ),  $i_0$  is the current exchange density ( $A/m^2$ ),  $V_m$  is the electrode potential(V),  $\Phi$  is the equilibrium potential(V),  $T$  is the absolute temperature(K),  $F$  is the Faraday constant,  $R$  is the universal gas constant,  $a_1$ =anodic charge transfer coefficient,  $a_2$ =cathodic charge transfer coefficient. In this model, the Tafel expressions are given by Turnbull for iron dissolution and hydronium reduction, i.e. [14]:

$$\text{Current density for iron oxidation, } i_1 = i_{01} \exp \left[ a_1 F \frac{(V_m - \Phi)}{RT} \right] \quad (3)$$

$$\text{Current density required for proton decrement, } i_2 = i_{02} [H] \exp \left[ a_2 F \frac{(V_m - \Phi)}{RT} \right] \quad (4)$$

Where  $i_{01}, i_{02}$  exchange current density ( $A/m^2$ ) for iron dissolution and hydrogen reduction respectively,  $i_1, i_2$  electrode current density ( $A/m^2$ ) for iron dissolution and hydrogen reduction respectively,

#### MODEL ASSUMPTIONS

In order to simulate the corrosion phenomenon of a single pit, specific assumptions are established initially, which are mentioned below:

- (i) Transport equations for dilute solution theory are considered and ignoring the interactions between dissolved chemical.
- (ii) Effects from the transport of aqueous chemical species due to convection are neglected.
- (iii) Effects of a double layer are not considered, and local electroneutrality within the pit electrolyte is assumed.
- (IV) Alloying ingredient are not considered (e.g., nickel or chromium). Only iron is considered as it is the greatest constituent in carbon steel.
- (V) mass transport in through-thickness was neglected.

#### REACTIONS

The reactions taking place are classified depending on the place where they occur. So, the reactions that take place at the electrode are represented as electrochemical reactions, while the reactions that occur at the solution are represented as homogeneous reactions [15].

##### Electrochemical reactions

The corrosion model of a pit is composed of three electrochemical reactions; the metal dissolution (anodic) process for the active wall is given by:



The reactions that occur at the cathode are described by oxygen reduction in eq (6) and hydrogen reduction in eq (7).



##### Homogeneous reactions

The homogeneous reactions in the solution are iron hydrolysis in Equation (8), water dissociation in Equation (9), with an addition of two more reactions are a product of the  $FeCl^+$  complex in equation (10), and hydrogen gas formation  $H_2$  by an electrochemical decrement in Equation (7).



Because of the bulk chlorine solution, the  $FeCl^+$  complex was used in the model. It is added for hydrogen gas production because hydrogen is a result of cathodic reactions and can be formed even though the possibility is anodic [17]. Sodium ions in sodium chloride solution are not included in the chemical reaction but are included to keep the electroneutrality across the mouth of pitting:



Depending to Sharland, six aqueous chemical species have been essential to creating a basic iron corrosion model; moreover, two other species added by [18,19]:  $Fe^{+2}$ ,  $H^+$ ,  $OH^-$ ,  $Cl^-$ ,  $Na^+$ ,  $FeOH^+$ ,  $FeCl^+$  and  $H_2$

#### BOUNDARY CONDITION

This paradigm is only investigated within the pit, and it is ignored outside of it. The fluxes of the ions included in the electrochemical oxidation at the pit's tip and bulk amount at the mouth are the boundary cases assumed in the pit model. At the passive wall, no reduction or dissolution occurs that is mean no production or depletion of ion occur as below:

$$\text{At the mouth of pit} \quad C_i = C_{i0} \quad \nabla \Phi = 0 \quad (12)$$

$$\text{At passive wall} \quad D_{Cl^-} [\nabla^2 C_{Cl^-} - \frac{F}{RT} \nabla(C_{Cl^-} \nabla \Phi)] = 0 \quad (13)$$

$$\text{At active wall} \quad D_{Cl^-} [\nabla^2 C_{Cl^-} - \frac{F}{RT} \nabla(C_{Cl^-} \nabla \Phi)] = \frac{i_1}{ZF} \quad (14)$$

$$D_{Cl^-} [\nabla^2 C_{Cl^-} - \frac{F}{RT} \nabla(C_{Cl^-} \nabla \Phi)] = \frac{i_2}{ZF} \quad (15)$$

Whereas;  $C_i$  is the species' amount,  $C_{i0}$  is the bulk amount.

#### NUMERICAL METHOD

The governing equations were solved numerically using COMSOL Multiphysics 3.5a depending on the finite-element technique. COMSOL Multiphysics is an effective interactive kit designed for modelling and solving all kinds of problems in science and engineering. The pit is presented in rectangular geometry with a curved bottom (set as electrochemically active). In the figure below illustrate the mesh of geometry that contain 325 mesh point and 582 elements.

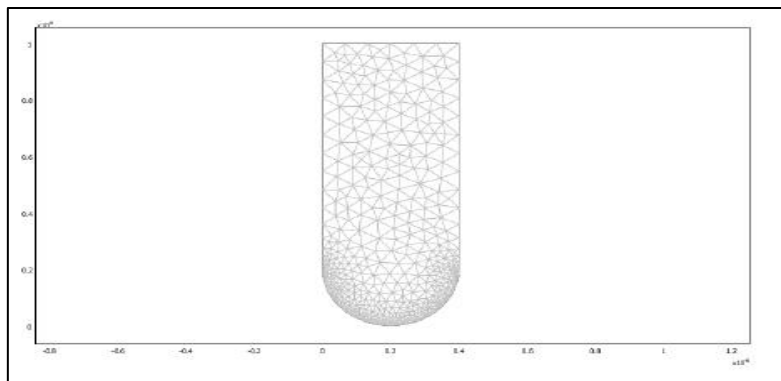


Figure 1. Mesh geometry of the pit

RESULT AND DISCUSSION

In this section, a part of what was obtained from the modelling program is shown with a simple explanation of the presented figures. From Figure 2 below, the ferrous ion ( $Fe^{+2}$ ) concentration observes a gradual rise with increasing applied potentials due to an increasing electrochemical rate of the metal dissolution process. At the mouth, which acts as bulk concentration,  $Fe^{+2}$  remains constant while increasing inside and bottom of the pit since the pit's bottom is electrochemically active where the dissolution of iron occurs.

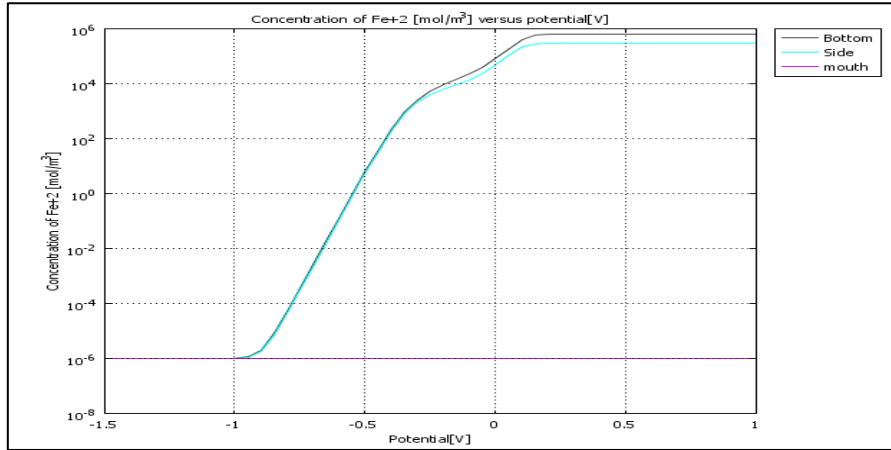


Figure 2. Amount of  $Fe^{+2}$  at three-point along with the pit.

The increase in iron dissolution from the bottom will make the region rich in positive charges, which causes the negative ions (chlorine ion) to migrate from the bulk to attract positive charges, as shown in figure (3) concentration increases in bottom and side as potential increase. Figure 4 shows the electrolyte pH at the electroactive surface (bottom of the pit) as a function of metal potentials, where the electrolyte experiences a rise in the pH with increasing cathodic potential. At lower anodic potentials, a steep drop in pH is observed, which can be referred to as an increased metal hydrolysis rate. Despite the sudden drop, the pH profile observes a slope change (from -0.6 V onwards) at higher anodic potentials. The potential electrolyte influences the metal dissolution process resulting in fewer  $Fe^{+2}$  ions ready to undergo hydrolysis. This, subsequently, cause fewer productions of protons, causing the pH to observe smaller changes.

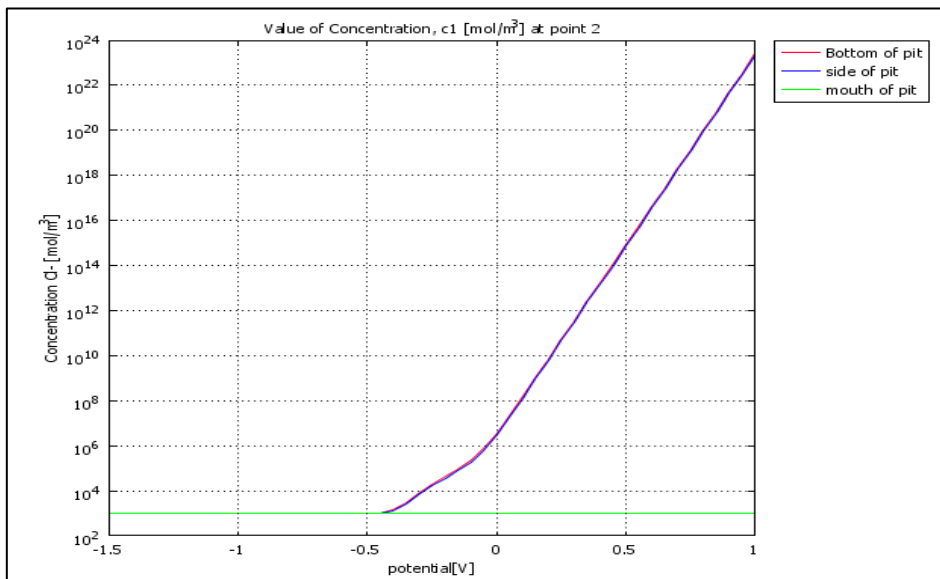
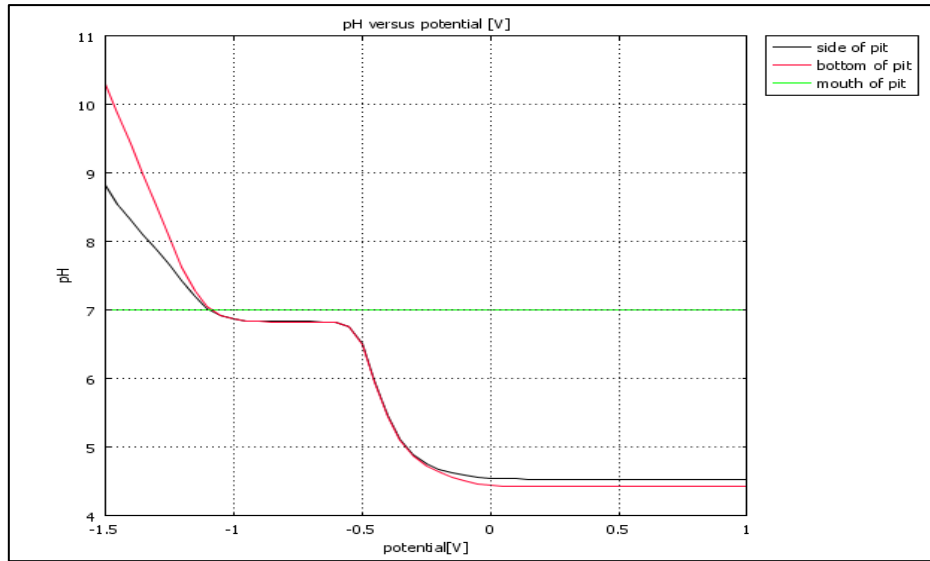
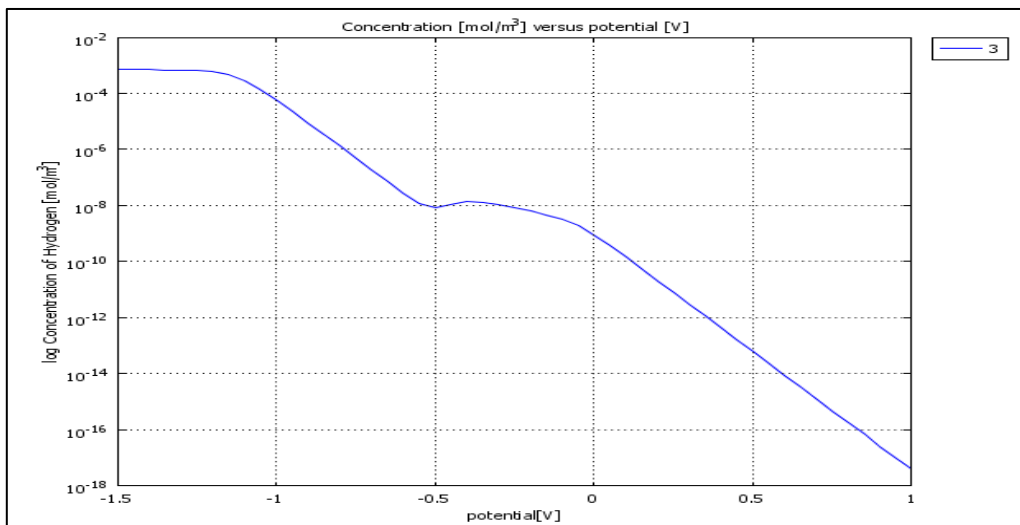


Figure 3. Amount of  $Cl^-$  at three-point along with pit



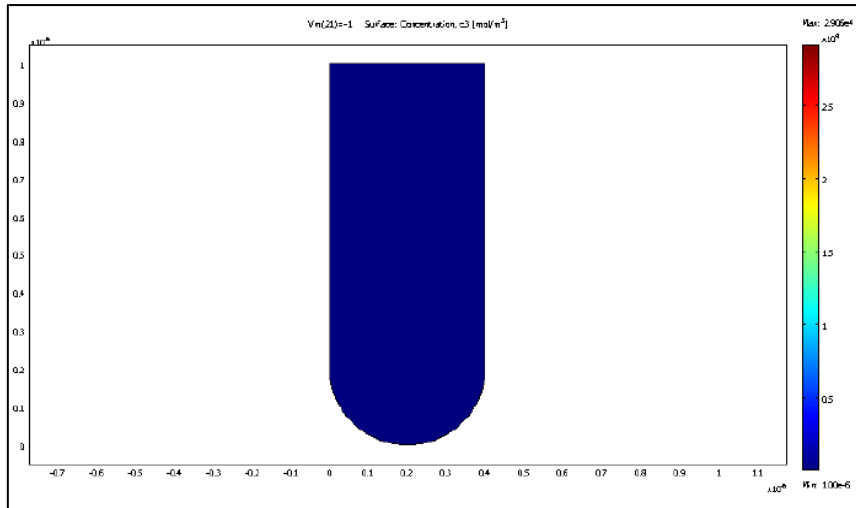
**Figure 4.** Electrolyte pH profile as a function of metal potentials at three-point along pitting.

It is possible to see the hydrogen bubbles as iron alloys are immersed in an acidic solution and are inactive. Metal ion  $Fe^{+2}$  is formed immediately, and hydrogen ions are decreased at the same time. This is a simple operation, and hydrogen gas should be noticeable at this stage. This is shown by the model in Figure 5, which depicts a rapid 'jump' in the 'amount' of hydrogen gas due to hydrogen to proton reductions.

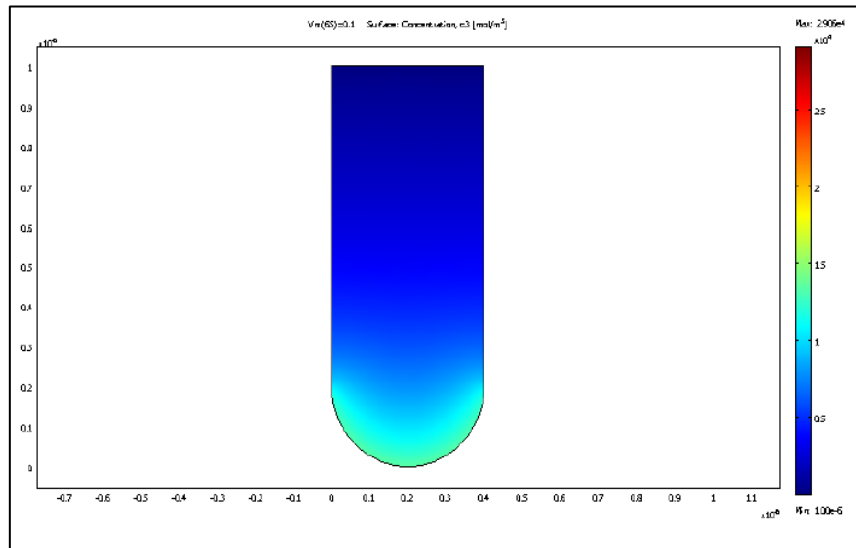


**Figure 5.** Amount of Hydrogen as a potential role at the bottom of pitting.

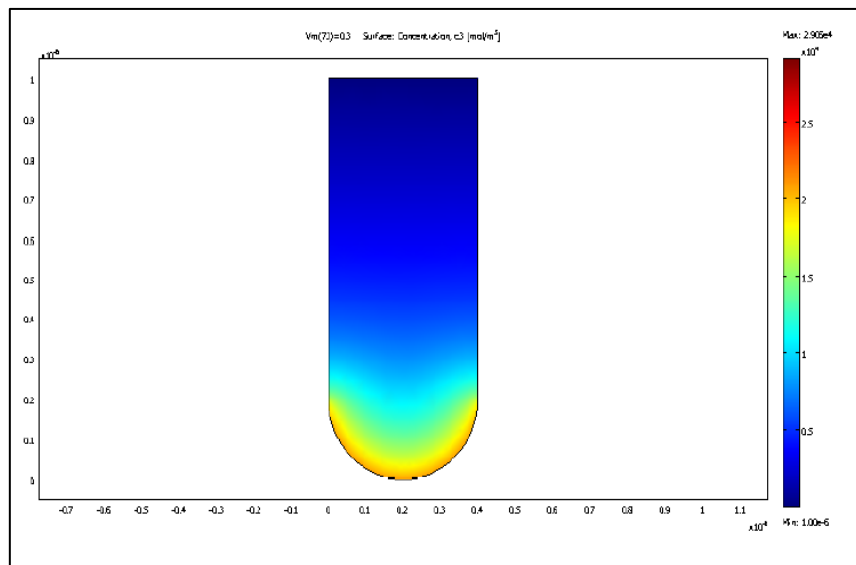
Figure 6 indicates that at the bottom of the trap, metal ions  $Fe^{+2}$  continue to accumulate slowly. The model is set to be electrochemically active in this field. The increasing amount of  $Fe^{+2}$  at the pit's bottom indicates that metal dissolution is continuing.  $Fe^{+2}$  continues to accumulate at the greater part of the hole, which could also be seen in the figure. This is consistent with diffusion, which states that animals migrate from high to low concentrations. In this scenario, the amount of  $Fe^{+2}$  has reached a point where the ions of metal diffuse to the passive area further up the pit, where the amount of  $Fe^{+2}$  is smaller. As described by,  $Fe^{+2}$  is supposed to hit a stage where it can disperse out of the trap, encouraging metal dissolution and forming general corrosion on the metal surface [20]. The effect of the potential is also shown in the figure below) fig.6), in which the dissolution density rises as the potential grows more optimistic.



(i) Amount of  $Fe^{+2}$  potential at -1 volt

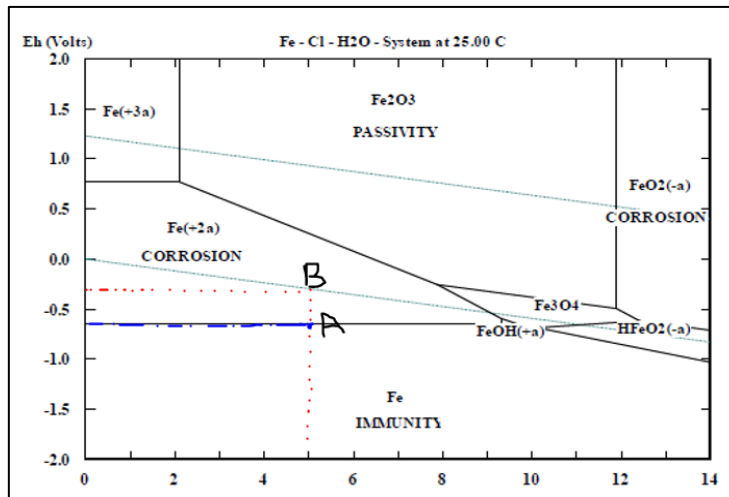


(ii) Amount of  $Fe^{+2}$  potential at 0.1 volt

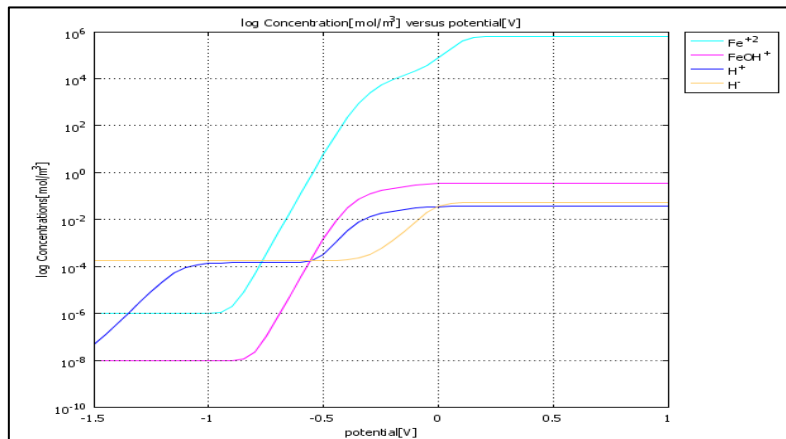


(iii) Amount of  $Fe^{+2}$  at potential 0.3 volt

Figure 6. Figures (i)-(iii) show that  $\text{Fe}^{+2}$  accumulation happens at the pit's bottom concerning potential. From Figure 5, it is found that hydrogen gas decreases almost suddenly, starting from -0.3. If this value is compared with the Pourbaix diagram in Figure 7, it is found to be intersecting at point A where water is thermodynamically stable instead of hydrogen, while the hydrogen is stable under this point. Hydrolysis is one of the most important reactions considered in the model, where water reacts with  $\text{Fe}^{+2}$  to create  $\text{H}^+$  and  $\text{FeOH}^+$ . This means that the reaction continues with the continuation of iron dissolution, as shown in Figure 8 that this reaction begins to occur at approximately -0.65[V]. If this value is compared with the Pourbaix diagram in Figure 7, it is found to be intersecting at point B, which is located between immunity and corrosion zone, and this shows that  $\text{Fe}^{+2}$  ion is produced at such condition (pH and potential).



**Figure 7.** Pourbaix schematic diagram point A, in which the model shows a metal ion predominance,  $\text{Fe}^{+2}$ . Furthermore, B, in which the model depicts the depletion of hydrogen gas,  $\text{H}_2$  [21]s.



**Figure 8.** Concentration of species as a function of potential

## CONCLUSION

The model's regulating formula in this study is based on anodic dissolution and transportation kinetics in the electrolyte. The model shows the importance of each parameter that was introduced in the model, how iron dissolution is affected by other equilibrium reactions, the effect of each on the other, the acidity of the medium and the initial concentrations of each species, the extent to which the potential range is affected., and finally to what a degree the results are consistent with what has been investigated in the literature.

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